Final Exam J. Graham

Dec. 14, 2012 Probability & Statistics

Instructions: There are twelve questions of equal value. Be sure to clearly indicate your final answer or conclusion. Probability answers can be given as fractions or in decimal form (rounded to four decimal places). Give units whenever units are involved.

- Q1. A cumulative frequency polygon is shown here.
 - a) Sketch the corresponding relative frequency polygon.
 - b) Estimate the mean of the sample.



- Q2. Ranked data is given in the table.
 - a) Determine the following statistics:
 - i) The Interquartile Range
 - ii) The sixtieth percentile
 - b) Use the Empirical Rule to determine if this sample data is approximately normally distributed.
- **Ranked Data** 28 28 30 31 32 34 36 37 40 42 42 42 43 38 39 41 44 44 46 47 47 47 49 54 55 55 56 59 65 61 64 68
- Q3. The number of days y required for concrete to cure was measured at various temperatures $x C^{\circ}$.
 - a) How many days do you predict for concrete to cure at 14 C°?
 Round off to one decimal place.
 - b) Interpret the slope of the prediction line.
 - c) Calculate and interpret the coefficient of determination.

Q4. Approximately 25% of Canadian men in their 50's have prostate cancer. High levels of prostate specific antigen (PSA) in blood is used as a test for prostate

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Q1.a)



b)

Q2. a) i) IQR = Q3 - Q1 = 54.5 - 37.5 = 17 ii) $P_{60} = x_{20} = 47$

- Q3. a) $\hat{y} = 28.004 0.5427x$ days. At x = 14 C°, $\hat{y} = 20.4$ days. We predict that it will take about 20.4 days for the concrete to cure at 14 C°.
- b) slope = -0.5427 tells us that curing time goes down by 0.5427 days for every increase of one degree in temperature.

Q5 a) = 1,
$$P(x) = \frac{\mu^x \cdot e^{-\mu}}{x!} = \frac{1^x \cdot e^{-1}}{x!}$$
 Px 3 = 1 P0 P1 P2 = 0.0803

b)

Q8. a)

 $H_o: \mu$ 0.08 ppmUse the μ - distribution because the population $H_a: \mu > 0.08$ ppmstandard deviation is unknown.

df = 59, $m_{0.10} = 1.296$, rejection region $m_{c} = 1.296$

$$\mathbf{x} = \frac{0.086 - 0.08}{\left(0.0331/\sqrt{60}\right)} = 1.404$$
 rejection region

Decision: Reject H_o Conclusion: At 10% Q11.

a) Use the *x*- distribution because the population standard deviations are unknown.

df = 69, $\mathbf{m}_{0.025} = 1.995$, $\overline{x}_{no pain} - \overline{x}_{pain} = 91.5 - 88.3 = 3.2 = one - point estimate$ $s_{pooled}^2 = \frac{33 \cdot 5.54^2 + 36 \cdot 7.82^2}{33 + 36} = 46.58419$, $E = (1.995) \cdot \sqrt{\frac{46.58419}{34} + \frac{46.58419}{37}} = 3.2348 \text{ degrees of lateral motion}$ The 95% C.I.E. is $-0.03 < \mu_{no pain} - \mu_{pain} < 6.43$ degrees of lateral motion.

b) Zero is in the interval, so it is possible that there is no difference. It is possible that $\mu_{no pain} = \mu_{pain}$

Q12. a)